

AD-A054 735

ARMY ARMAMENT RESEARCH AND DEVELOPMENT COMMAND ABERD--ETC F/G 19/1
AEROBALLISTICS OF CORKSCREW PROJECTILES.(U)

UNCLASSIFIED

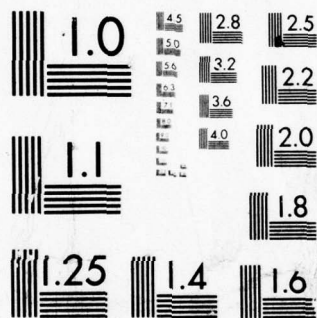
ARBRL-MR-02825

SBIE-AD-E430 032

NL

OF
AD
A054735





MICROCOPY RESOLUTION TEST CHART
NATIONAL BUREAU OF STANDARDS-1963-A

FOR FURTHER TRAN

18 May 78

AD-E430 032

AD A 054735

MEMORANDUM REPORT ARBRL-MR-02825

(Supersedes IMR No. 541) ^{NT}

AEROBALLISTICS OF CORKSCREW PROJECTILES

Anders S. Platou

April 1978

AD No. ^{7C} FILE COPY



US ARMY ARMAMENT RESEARCH AND DEVELOPMENT COMMAND
BALLISTIC RESEARCH LABORATORY
ABERDEEN PROVING GROUND, MARYLAND

Approved for public release; distribution unlimited.

DDC
RECEIVED
JUN 6 1978
B

Destroy this report when it is no longer needed.
Do not return it to the originator.

Secondary distribution of this report by originating
or sponsoring activity is prohibited.

Additional copies of this report may be obtained
from the National Technical Information Service,
U.S. Department of Commerce, Springfield, Virginia
22161.

The findings in this report are not to be construed as
an official Department of the Army position, unless
so designated by other authorized documents.

*The use of trade names or manufacturers' names in this report
does not constitute indorsement of any commercial product.*

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER MEMORANDUM REPORT	2. GOVT ACCESSION NO. ARBRL-MR-02825	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle) AEROBALLISTICS OF CORKSCREW PROJECTILES.	5. TYPE OF REPORT & PERIOD COVERED Final rept.	6. PERFORMING ORG. REPORT NUMBER
7. AUTHOR(s) Anders S. Platou	8. CONTRACT OR GRANT NUMBER(s)	9. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS RDT&E 1L161102AH43
9. PERFORMING ORGANIZATION NAME AND ADDRESS U.S. Army Ballistic Research Laboratory (ATTN: DRDAR-BLL) Aberdeen Proving Ground, MD 21005	10. REPORT DATE APR 1978	11. NUMBER OF PAGES 35
11. CONTROLLING OFFICE NAME AND ADDRESS US Army Armament Research & Development Command US Army Ballistic Research Laboratory (ATTN: DRDAR-BL) Aberdeen Proving Ground, MD 21005	12. SECURITY CLASS. (of this report) Unclassified	13. DECLASSIFICATION/DOWNGRADING SCHEDULE
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office) 1230p.	15. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited. 18 SBIE	
16. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report) 19 AD-E430-032		
17. SUPPLEMENTARY NOTES This BRL Memorandum Report supersedes BRL Interim Memorandum Report No. 541 dated February 1977.		
18. KEY WORDS (Continue on reverse side if necessary and identify by block number) Projectile Aeroballistics Aerodynamics Gyroscopic Stability		
19. ABSTRACT (Continue on reverse side if necessary and identify by block number) (1cb) Preliminary wind tunnel and aeroballistic range tests on a new and novel exterior projectile shape have shown that this 5-caliber long shape has extremely good aerodynamic characteristics. It not only has very low drag, but also low pitching and Magnus moments which in turn yield good gyroscopic and good dynamic stability. Extrapolation of the data to longer lengths indicates that 10-caliber to 12-caliber long projectiles having this shape can be flown with satisfactory stability.		

DD FORM 1473 EDITION OF 1 NOV 65 IS OBSOLETE

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

393472

B

TABLE OF CONTENTS

	<u>Page</u>
LIST OF ILLUSTRATIONS	5
LIST OF TABLES	6
I. INTRODUCTION	7
II. THE CORKSCREW GEOMETRY	7
III. TEST RESULTS	8
IV. EXTRAPOLATION TO LONGER LENGTH PROJECTILES	9
REFERENCES	27
LIST OF SYMBOLS	29
DISTRIBUTION LIST	33

ACCESSION TO		
NTIS	Value Section	<input checked="" type="checkbox"/>
DDC	Self Section	<input type="checkbox"/>
UNCLASSIFIED		<input type="checkbox"/>
JUSTIFICATION		
BY		
DISTRIBUTION/AVAILABILITY CODES		
Dist.	AVAIL.	and/or SPECIAL
A		

LIST OF ILLUSTRATIONS

<u>Figure</u>		<u>Page</u>
1.	The Corkscrew Projectile	11
2.	The 5-Caliber Wind Tunnel Model of the Corkscrew Projectile	12
3.	The Normal Force Coefficient of the Corkscrew Projectile	13
4.	The Pitching Moment Coefficient of the Corkscrew Projectile	14
5.	The Approximate Magnus Characteristics of the Corkscrew Projectile	15
6.	The 155mm M549 Projectile	16
7.	The Non-Conical Boattail Projectile (NCB-A)	17
8.	A Shadowgraph of a Corkscrew Projectile Flying at M = .92	18
9.	A Shadowgraph of a Conventional Projectile Flying at M = .92	19
10.	The Area Distribution of a Corkscrew Projectile Compared to a Conventional Projectile	20
11.	The Drag Coefficient of a Corkscrew Projectile Compared to Other Projectiles	21
12.	The Normal Force Coefficient of the Corkscrew Projectile Compared to Other Projectiles	22
13.	The Pitching Moment Coefficient of the Corkscrew Projectile Compared to Other Projectiles	23

LIST OF TABLES

Table	Page
I. Aerodynamic Characteristics of the 6-Caliber and 8-Caliber Corkscrews.	24
II. Aeroballistic Characteristics of the 6-Caliber and 8-Caliber Corkscrews.	25
III. Physical and Aerodynamic Characteristics	26
1. The Corkscrew Projectile	27
2. The 6-Caliber Projectile	28
3. The 8-Caliber Projectile	29
4. The Approximate Magnus Characteristics of the Corkscrew Projectile	30
5. The 155mm M59 Projectile	31
6. The Non-Conical Boretail Projectile (NCB-A)	32
7. A Shadowgraph of a Corkscrew Projectile Flying at $M = .92$	33
8. A Shadowgraph of a Conventional Projectile Flying at $M = .92$	34
9. The Area Distribution of a Corkscrew Projectile Compared to a Conventional Projectile	35
10. The Drag Coefficient of a Corkscrew Projectile Compared to Other Projectiles	36
11. The Normal Force Coefficient of the Corkscrew Projectile Compared to Other Projectiles	37
12. The Pitching Moment Coefficient of the Corkscrew Projectile Compared to Other Projectiles	38

I. INTRODUCTION

During the development and exploitation of the BRL Non-Conical Boattail Projectile¹⁻⁶, it became evident that a new projectile shape which combines a triangular nose with a triangular boattail (Figure 1) would have low drag and a long wheel base for low balloting in the gun barrel. No aerodynamic data were available on the configuration (nicknamed the corkscrew) at the beginning of this program, so it was deemed advisable to conduct wind tunnel and range tests to determine its drag and stability characteristics.

II. THE CORKSCREW GEOMETRY

The basic corkscrew geometric pattern is obtained by cutting a solid cylinder with six skewed planes to obtain the configuration shown in Figure 1. Three skewed planes form the pointed triangular nose and the other three skewed planes, sloped the opposite way, form the boattail. The boattail planes up to now have been terminated when they form an inscribed triangle, but it is possible to terminate them at any desired axial station. The slope or angle of these planes with respect to the cylinder centerline can be varied; however, the angles of the three nose planes must be the same as well as the angles of the

1. Anders S. Platou, "An Improved Projectile Boattail," Ballistic Research Laboratory Memorandum Report No. 2395, July 1974. AD 785520.
2. Anders S. Platou and George I. T. Nielsen, "An Improved Projectile Boattail. Part II," Ballistic Research Laboratory Report No. 1866, March 1976. AD A024073.
3. Anders S. Platou, "An Improved Projectile Boattail. Part III," Ballistic Research Laboratory Memorandum Report No. 2644, July 1976. AD B012781L.
4. John H. Whiteside, "Transonic Tests of the 155mm Non-Conical Boattail Projectile A and 8-Inch XM650E4 and EBVP Projectiles at Nicolet, Canada, During January-February 1977," Ballistic Research Laboratory Memorandum Report No. ARBRL-MR-02809, January 1978.
5. Vural Oskay and Anders S. Platou, "Yawsonde Tests of 155mm M549 Non-Conical Boattail Projectile at Tonopah Test Range," Ballistic Research Laboratory Memorandum Report in preparation.
6. Anders S. Platou, "Wind Tunnel, Aeroballistic Range, and Full Range Flight Tests of the Non-Conical Boattail Projectile A," Ballistic Research Laboratory Memorandum Report in preparation.

three boattail planes. The nose plane angles need not be the same as the boattail plane angles. The six planes are usually skewed at a constant twist rate generally near the spin expected at launch.

The corkscrew configuration does not have the usual axial symmetry and, therefore, it can be expected to have non-linear aerodynamic characteristics, especially at spins ($\rho d/V$) far from the configuration twist. For this reason, the spin of all of the range flights made to date have been near the twist of the configuration.

III. TEST RESULTS

The first data came from supersonic wind tunnel tests of a 5-caliber long non-interdigitated or non-overlapping configuration (Figure 2). This configuration has a 10° nose angle and a 7° boattail and the model is 5.715 cm in diameter. The significant results from these tests are described below and are compared with results from the 5-caliber Army-Navy Spinner Rocket (ANSR) with a cylindrical tail.

(a) Even though the normal force on the corkscrew is extremely high (Figure 3), the pitching moments about a center of gravity three calibers aft of the nose are about the same as those on the 5-caliber ANSR (Figure 4). Therefore, the normal force center of pressure of the corkscrew configuration is located further aft than on the 5-caliber ANSR.

(b) At low angles of attack, the Magnus forces and moments are small at all spin rates near the configuration twist. This is due to the zero-spin "offsetting" side force and moment characteristic of this configuration² (Figure 5).

Because of the difficulty in designing and building the interdigitated wind tunnel version, 20 mm diameter 6-caliber and 8-caliber long models were built for flights in the BRL Aerodynamics Range. The models were made of brass and used drilled base holes to increase the possibility of stable flights in the range. The 6-caliber long models had 7° triangular boattails and 5.71° triangular noses while the 8-caliber long models had 4.76° on both nose and boattail planes. Both the 6-caliber and 8-caliber configurations had one caliber overlap between the nose and boattail planes. Below, aerodynamic data from several flights up to $M = 2.2$ are compared with aerodynamic data on the 5.7-caliber long M549 (Figure 6) and the 6.2-caliber long non-conical boattail projectile-A (Figure 7).

(1) Shock waves or flow discontinuities on the corkscrew configuration appear to be virtually non-existent at transonic speeds (Figure 8). This figure can be compared to the shock wave pattern existing on a conventional projectile configuration at the same Mach number (Figure 9). The almost shock-free flow pattern is believed to be due to the

more uniform area distribution of the corkscrew configuration (Figure 10). Further studies in both ranges and wind tunnels would be necessary to completely understand and explain this phenomenon.

(2) The drag coefficient of the corkscrew configuration is very low compared to that of the two reference projectiles (Figure 11).

(3) The normal force coefficient (Figure 12) is not as large as for the non-interdigitated wind tunnel configuration, but it is larger than for the M549 and the NCB-A projectiles.

(4) Even with the rearward center of gravity of the corkscrews, the pitching moment coefficient is much lower for the 6-caliber corkscrew (Figure 13) than for the M549 and NCB-A projectiles. The pitching moment coefficient of the 8-caliber corkscrew is just slightly higher than the maximum pitching moment coefficient of the M549. The pitching moment coefficient of the corkscrew appears to remain nearly constant with Mach number, indicating that the corkscrew configuration does not have the characteristic spike in the pitching moment curve. Additional data above $M = 1.05$ are required to verify this.

(5) Efforts to fly corkscrews at higher Mach numbers have so far failed due to excessive loads on the model nose during launch. Various launching techniques are being tried to overcome this problem.

(6) The aerodynamic and aeroballistic coefficients of the corkscrew configurations obtained from the various flights are given in Tables I and II.

IV. EXTRAPOLATION TO LONGER LENGTH PROJECTILES

The aerodynamic data obtained on the corkscrew configurations indicate that longer configurations of this shape can be flown with satisfactory stability. The implication is that the corkscrew will permit the use of much longer, full bore, spin-stabilized, low drag projectiles.

Calculation of possible projectile lengths have been made and the results are shown in Table III. For the calculation of the moments of inertia, it was assumed that the corkscrew configuration has equal angles for the nose and tail "flats", that the nose and tail overlap by one caliber, and that the projectile is made of a homogeneous material with a density of 9 g/cm^3 . Using the obtained values for the 6-caliber and 8-caliber corkscrews, the normal force and pitching moment coefficients for longer configurations have been estimated at Mach 2.1 (Table III).

From these assumptions and calculations, the gyroscopic stability factor has been calculated. This calculation indicates that an 11-caliber corkscrew made of homogeneous material with a density of 9 g/cm^3 can be flown with satisfactory stability if the spin is at least one revolution per fifteen calibers of forward travel.

(2) The normal force coefficient (Figure 12) is not as large as for the non-indicated wind tunnel configuration, but it is larger than for the M42 and the M42-A projectiles.

(3) Even with the rearward center of gravity of the corkscrew, the pitching moment coefficient is much lower for the 8-caliber corkscrew (Figure 13) than for the M42 and M42-A projectiles. The pitching moment coefficient of the 8-caliber corkscrew is just slightly higher than the maximum pitching moment coefficient of the M42. The pitching moment coefficient of the corkscrew appears to remain nearly constant with Mach number, indicating that the corkscrew configuration does not have the characteristic spike in the pitching moment curve. Additional data above $M = 1.05$ are required to verify this.

(4) Efforts to fly corkscrews at higher Mach numbers have so far failed due to excessive loads on the model nose during launch. Various launching techniques are being tried to overcome this problem.

(5) The aerodynamic and aeroballistic coefficients of the corkscrew configurations obtained from the various flights are given in Tables I and II.

III. EXTRAPOLATION TO LONGER LENGTH PROJECTILES

The aerodynamic data obtained on the corkscrew configurations indicate that longer configurations of this shape can be flown with satisfactory stability. The implication is that the corkscrew will permit the use of much longer, full bore, spin-stabilized, low drag projectiles.

Calculation of possible projectile lengths have been made and the results are shown in Table III. For the calculation of the moments of inertia, it was assumed that the corkscrew configuration has equal length for the nose and tail halves, that the nose and tail overlap by one caliber, and that the projectile is made of a homogeneous material with a density of 9 g/cm^3 . Using the obtained values for the 8-caliber and 8-caliber corkscrews, the normal force and pitching moment coefficients for longer configurations have been estimated at Mach 3.1 (Table III).

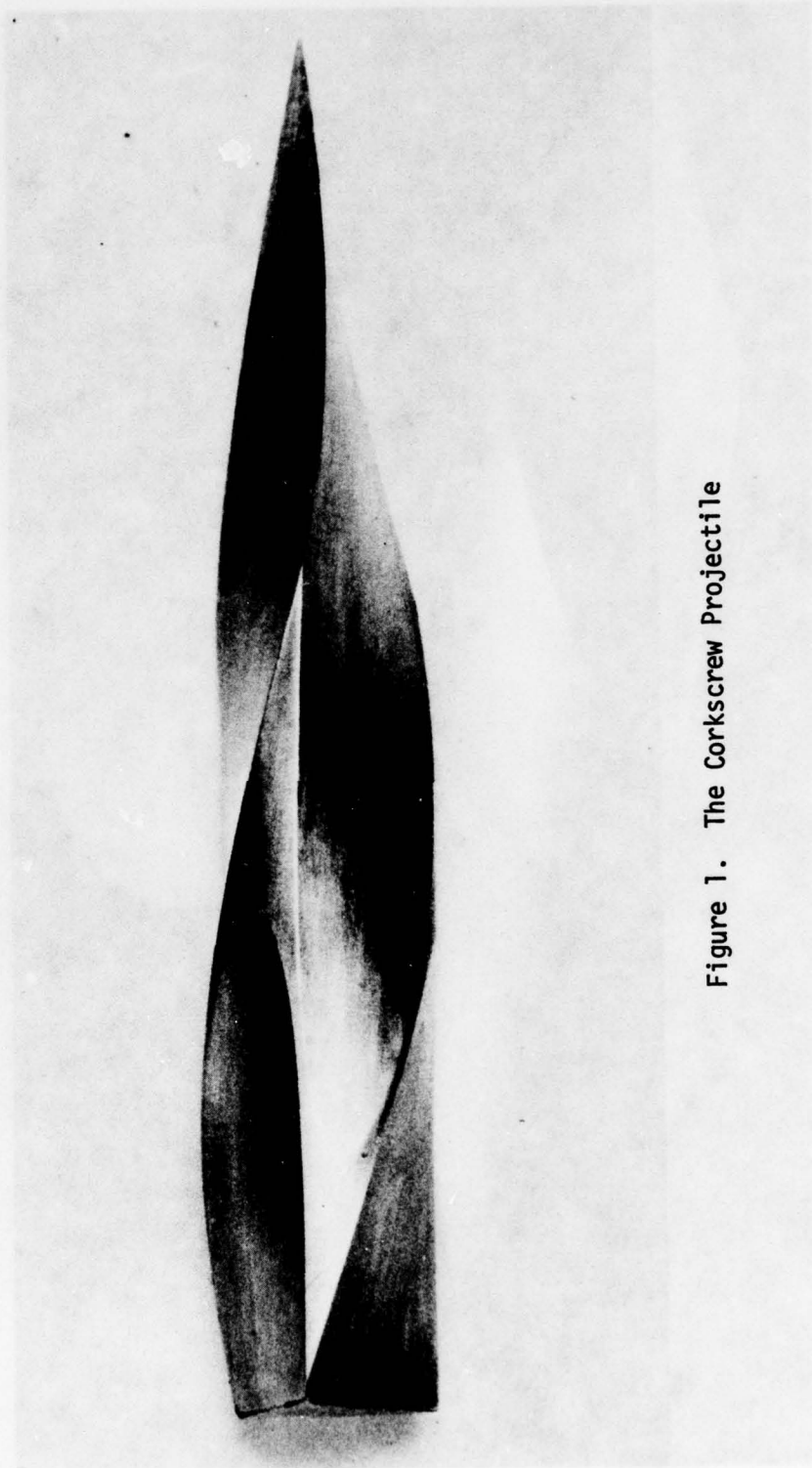


Figure 1. The Corkscrew Projectile

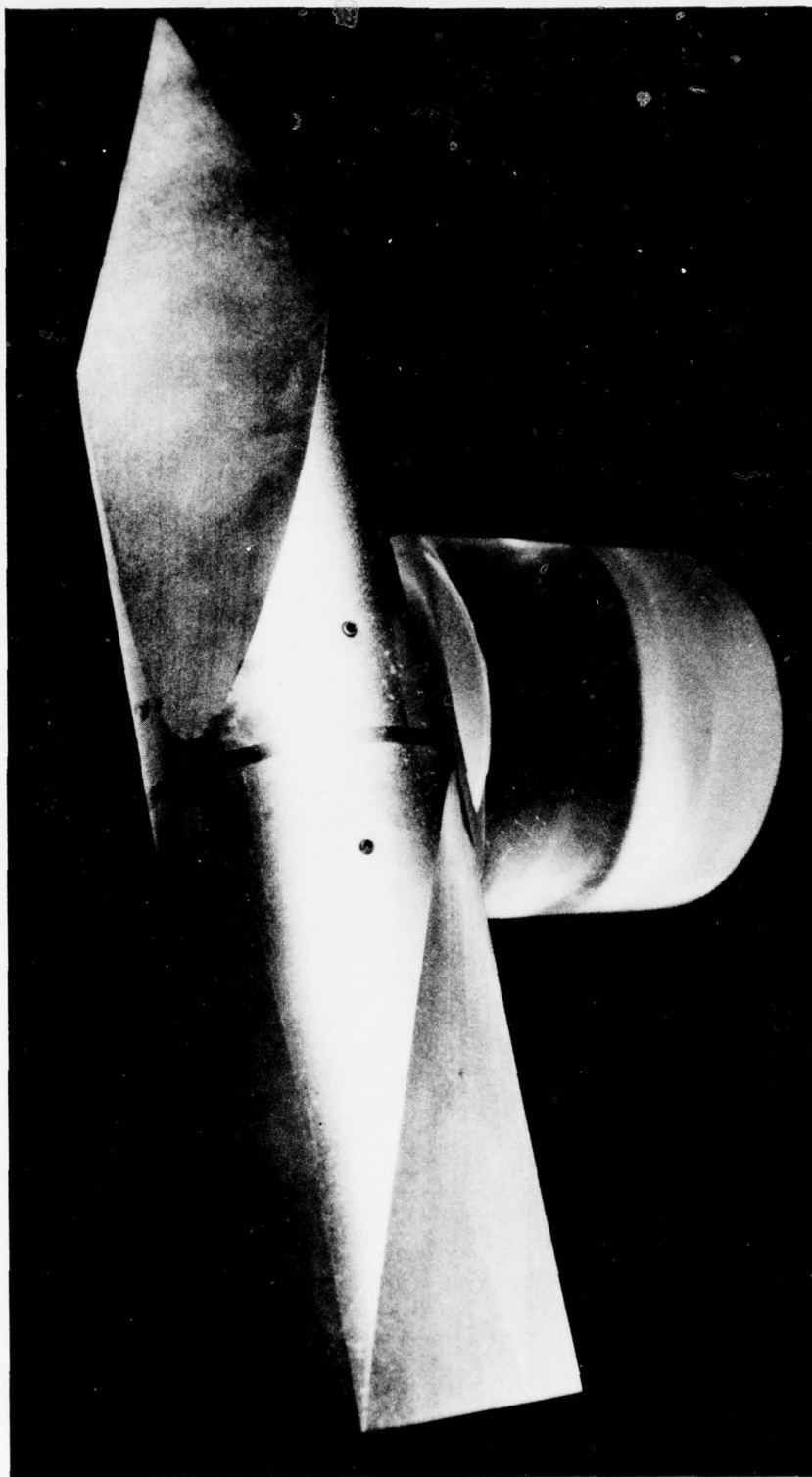


Figure 2. The 5-Caliber Wind Tunnel Model of the Corkscrew Projectile

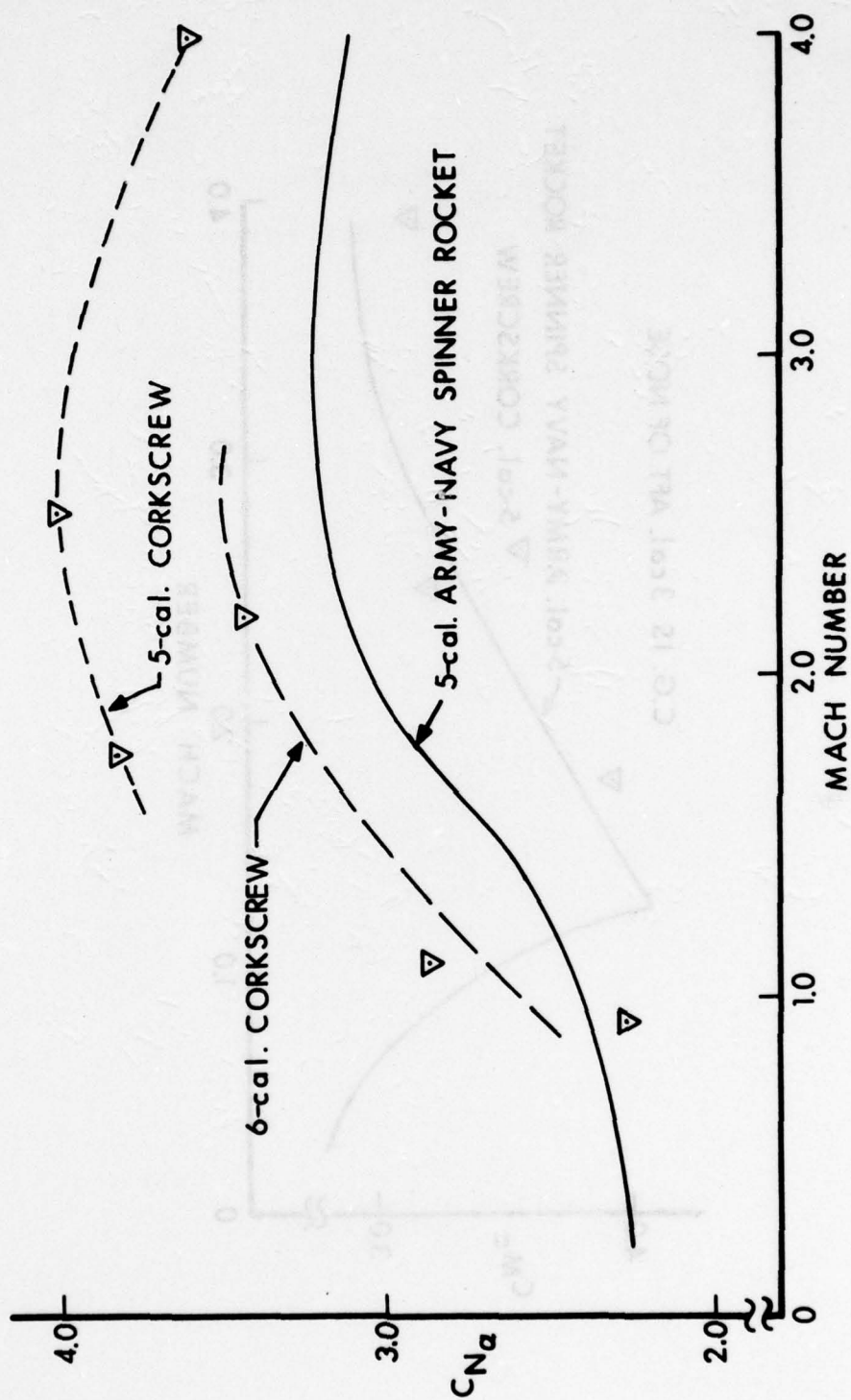


Figure 3. The Normal Force Coefficient of the Corkscrew Projectile

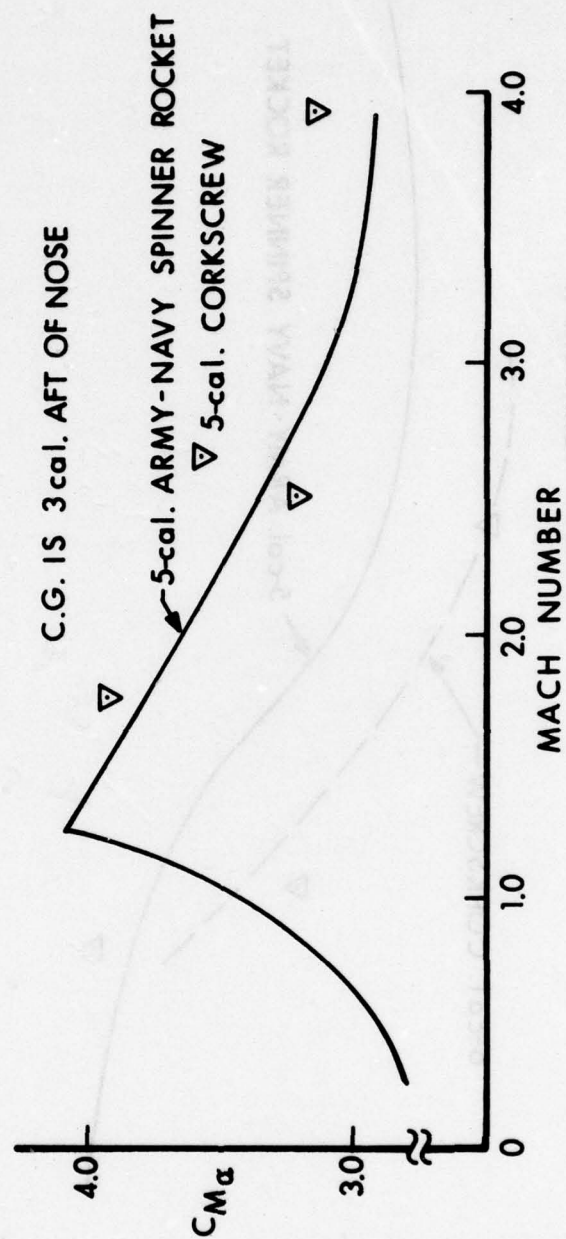


Figure 4. The Pitching Moment Coefficient of the Corkscrew Projectile

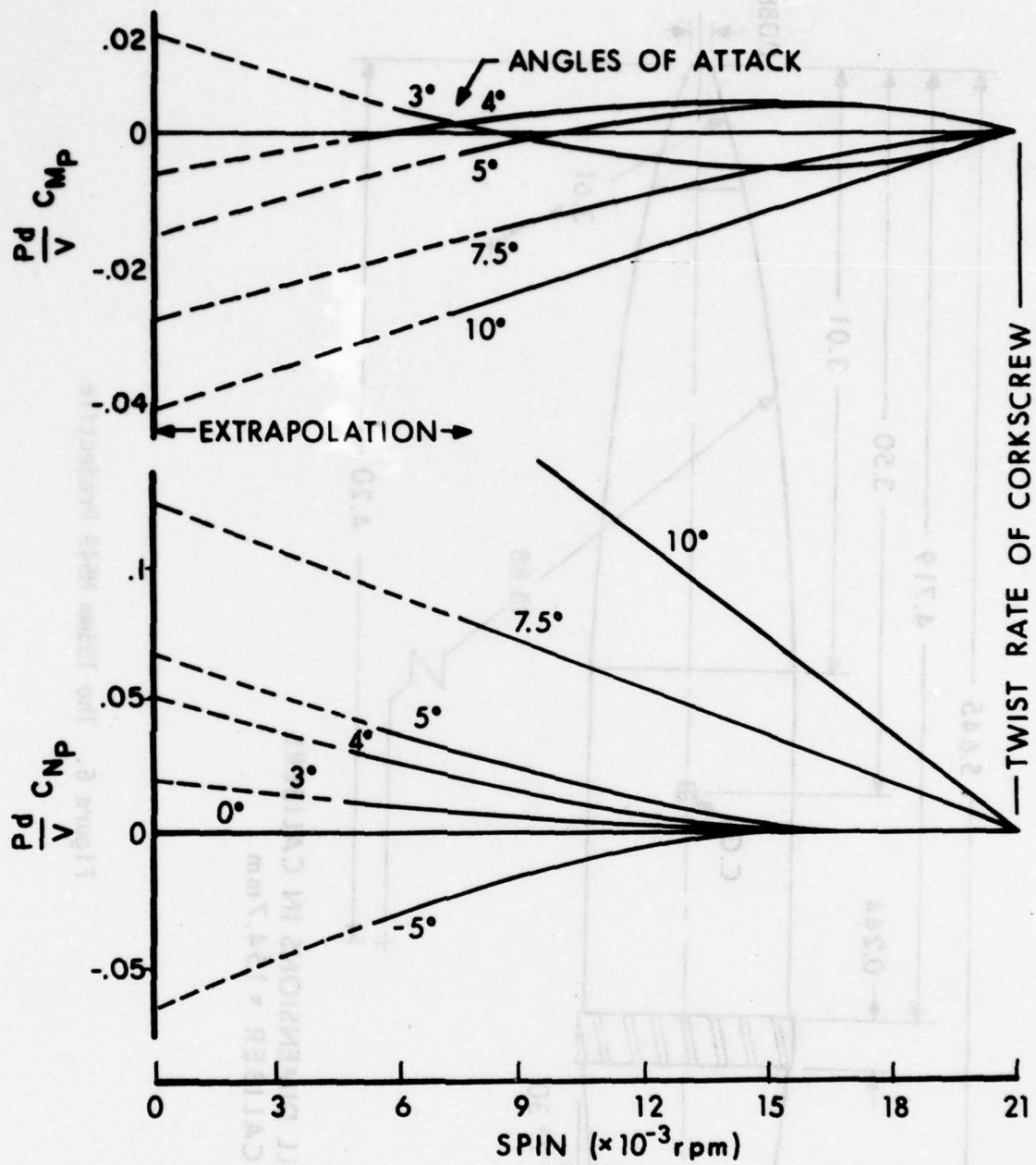


Figure 5. The Approximate Magnus Characteristics of the Corkscrew Projectile

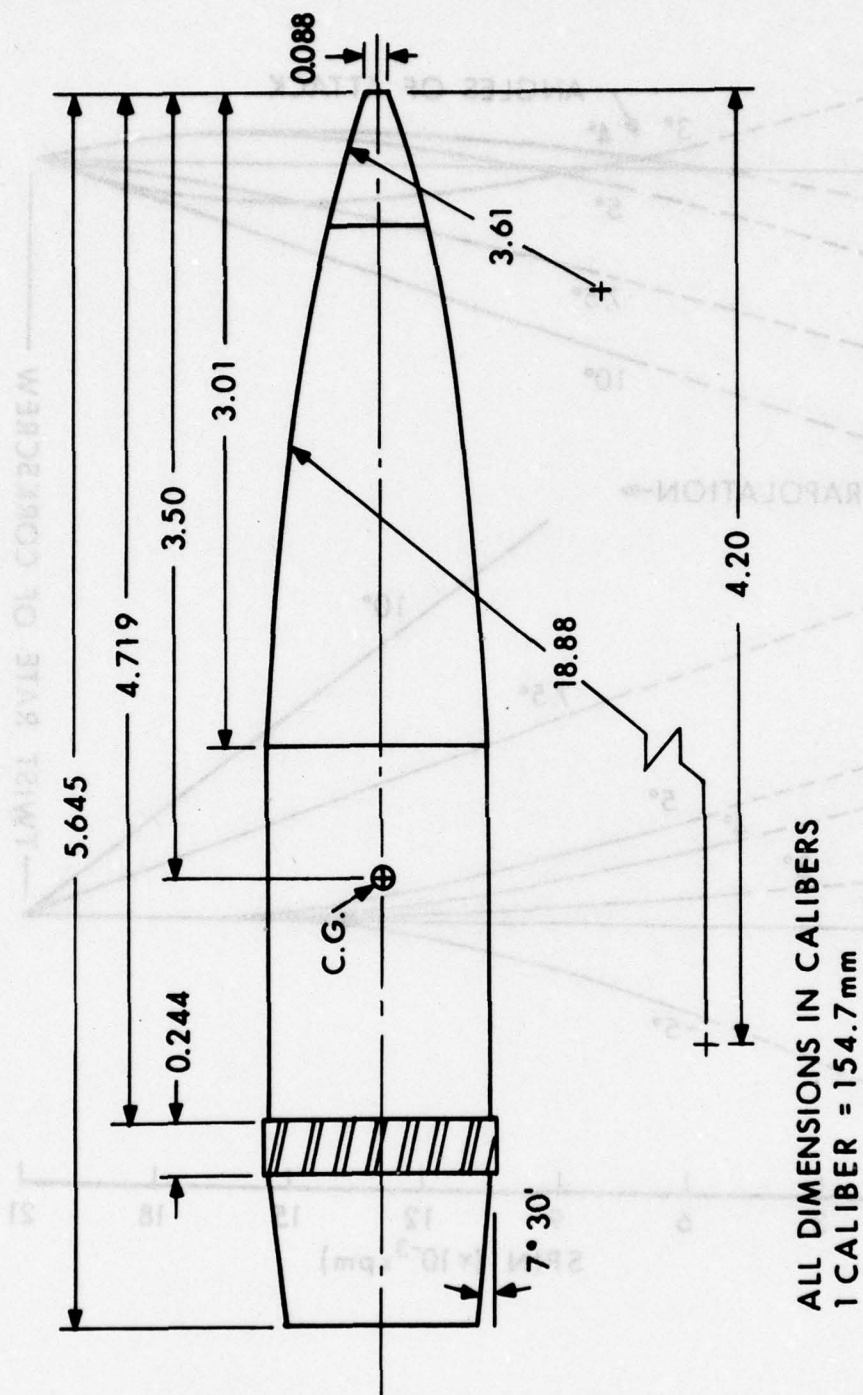


Figure 6. The 155mm M549 Projectile

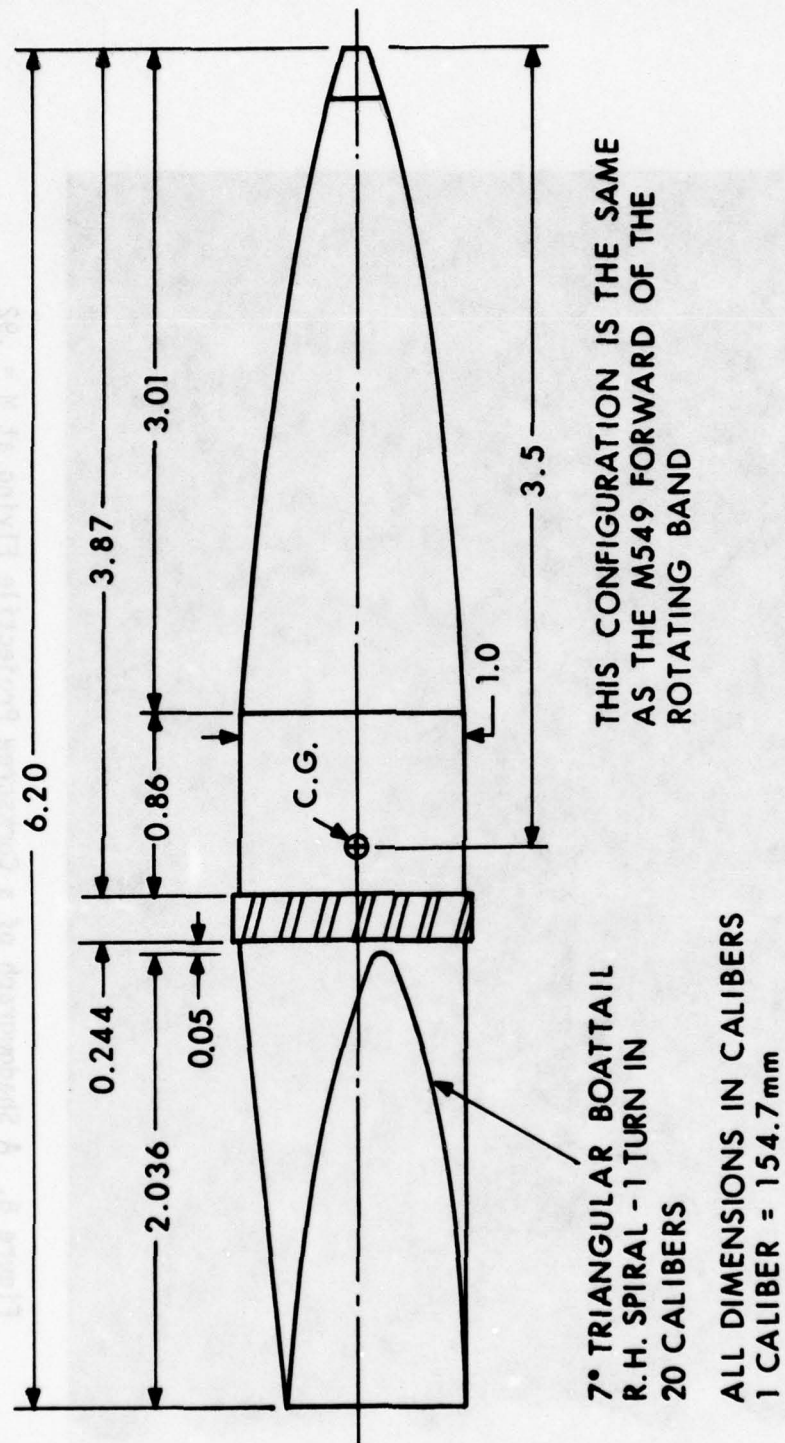


Figure 7. The Non-Conical Boattail Projectile (NCB-A)



Figure 8. A Shadowgraph of a Corkscrew Projectile Flying at $M = .92$

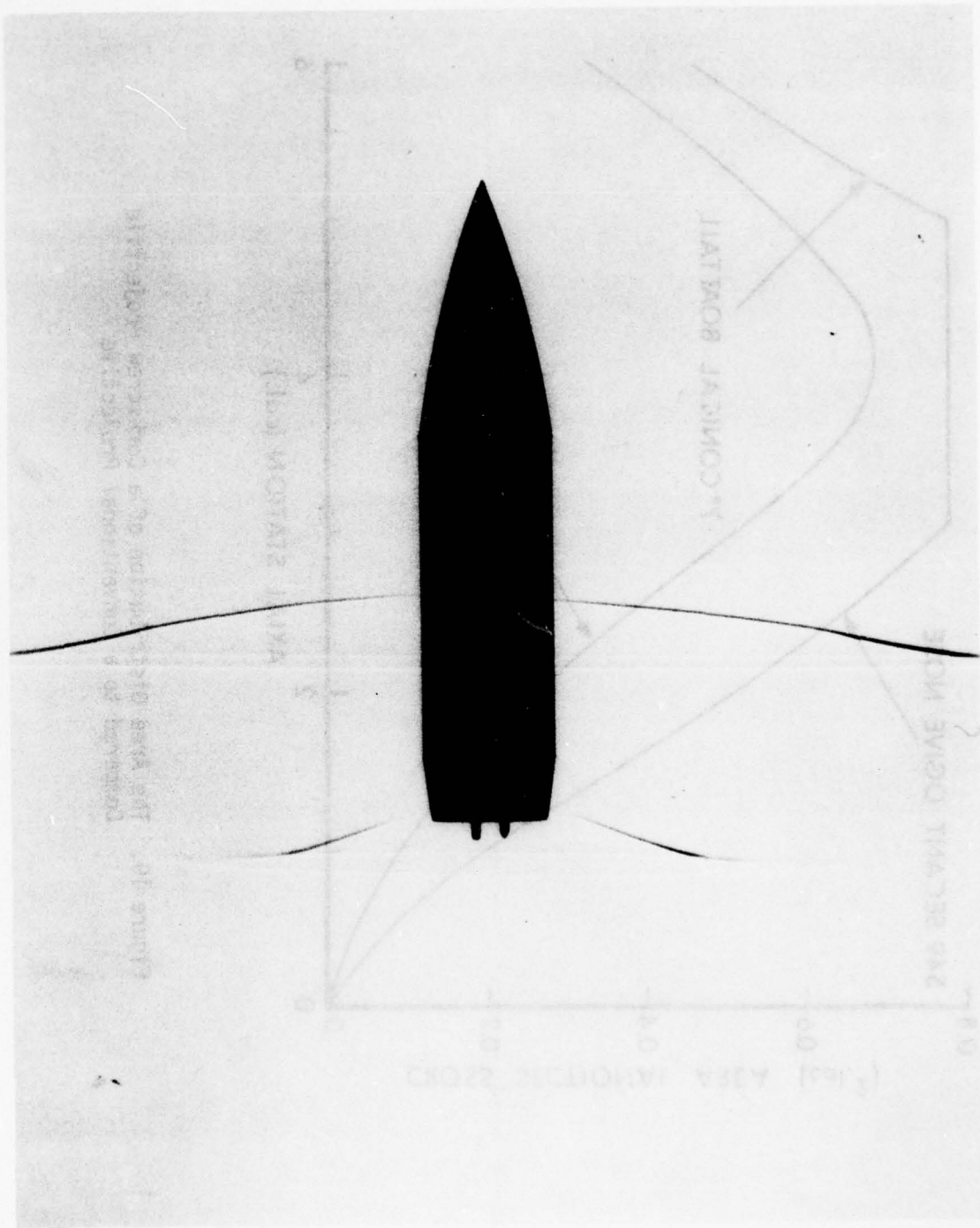


Figure 9. A Shadowgraph of a Conventional Projectile Flying at $M = .92$

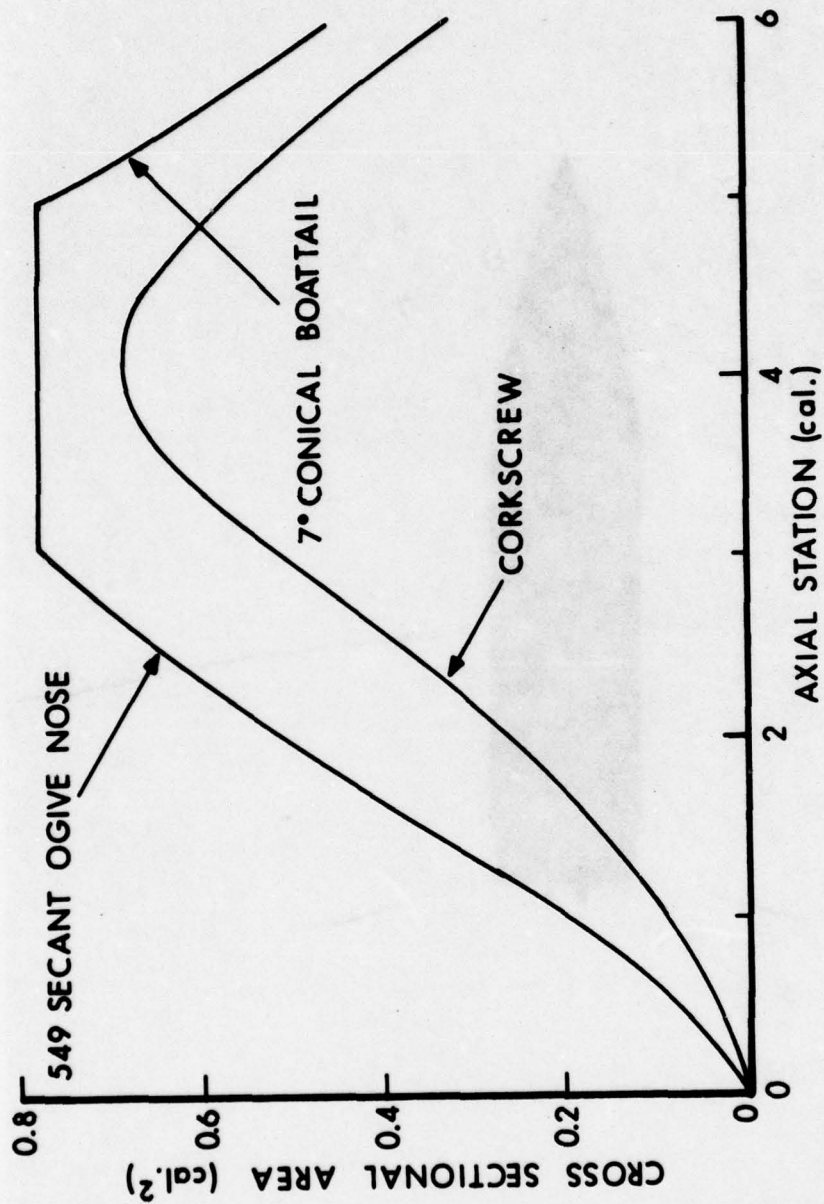


Figure 10. The Area Distribution of a Corkscrew Projectile Compared to a Conventional Projectile

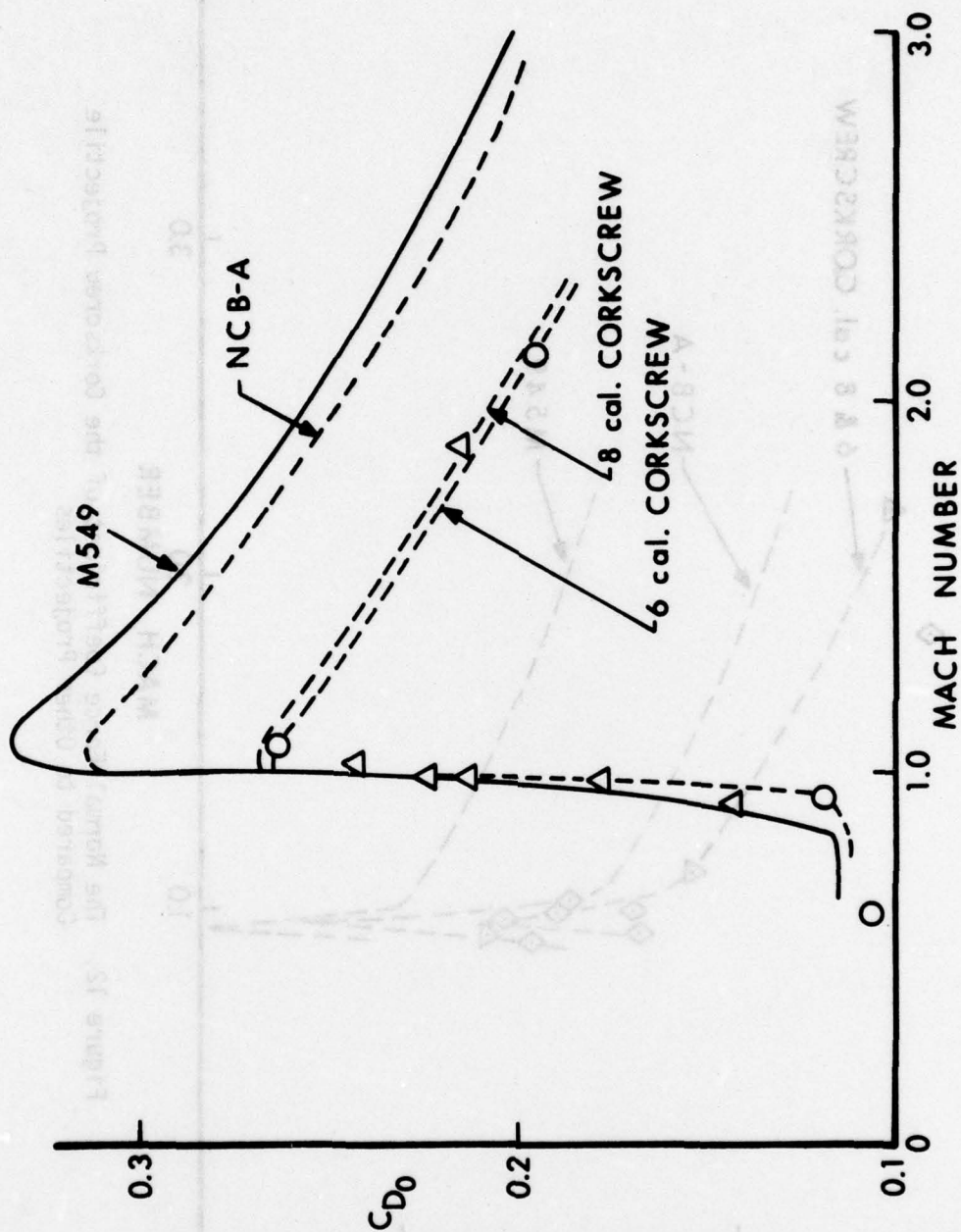


Figure 11. The Drag Coefficient of a Corkscrew Projectile/M Compared to Other Projectiles

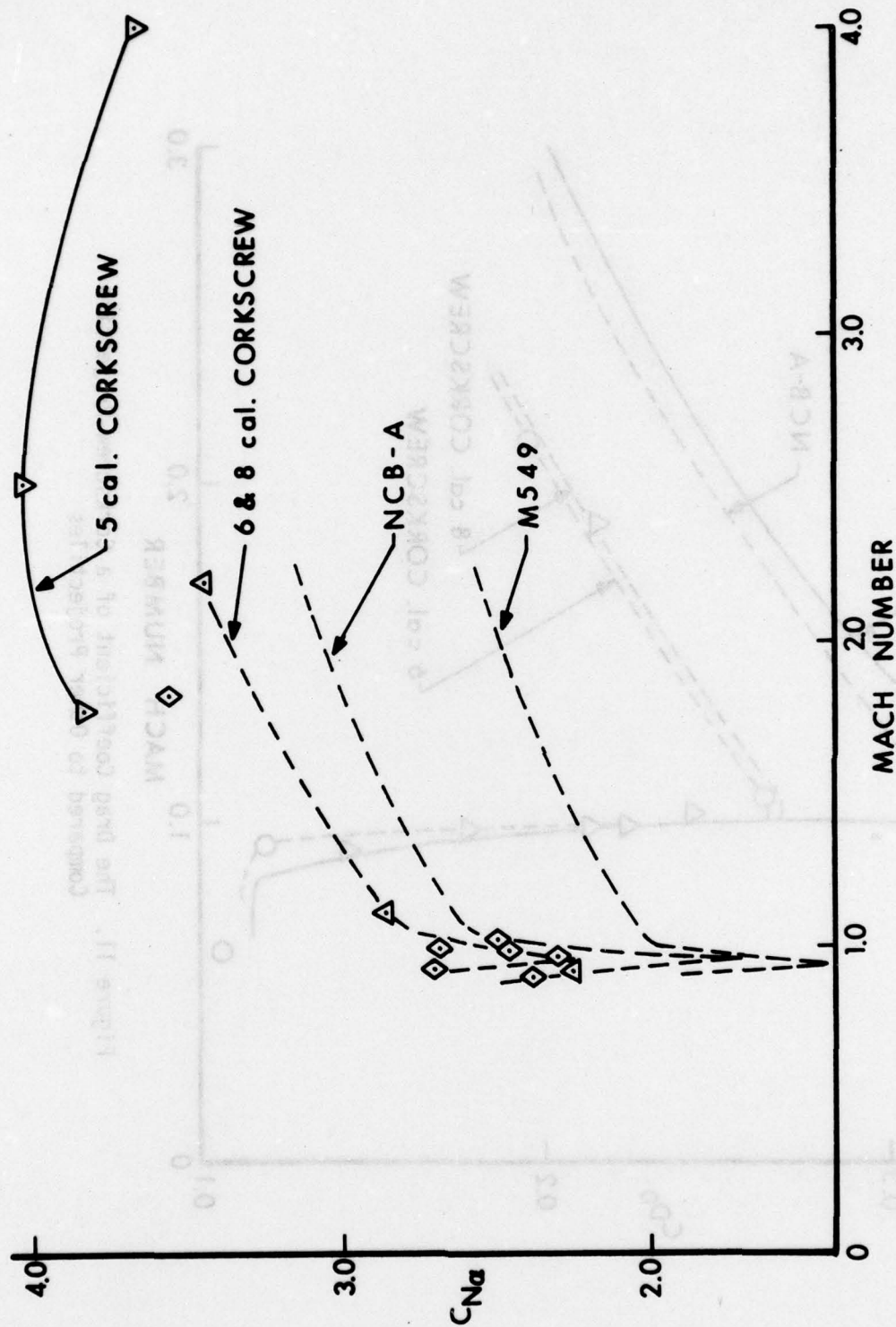


Figure 12. The Normal Force Coefficient of the Corkscrew Projectile Compared to Other Projectiles

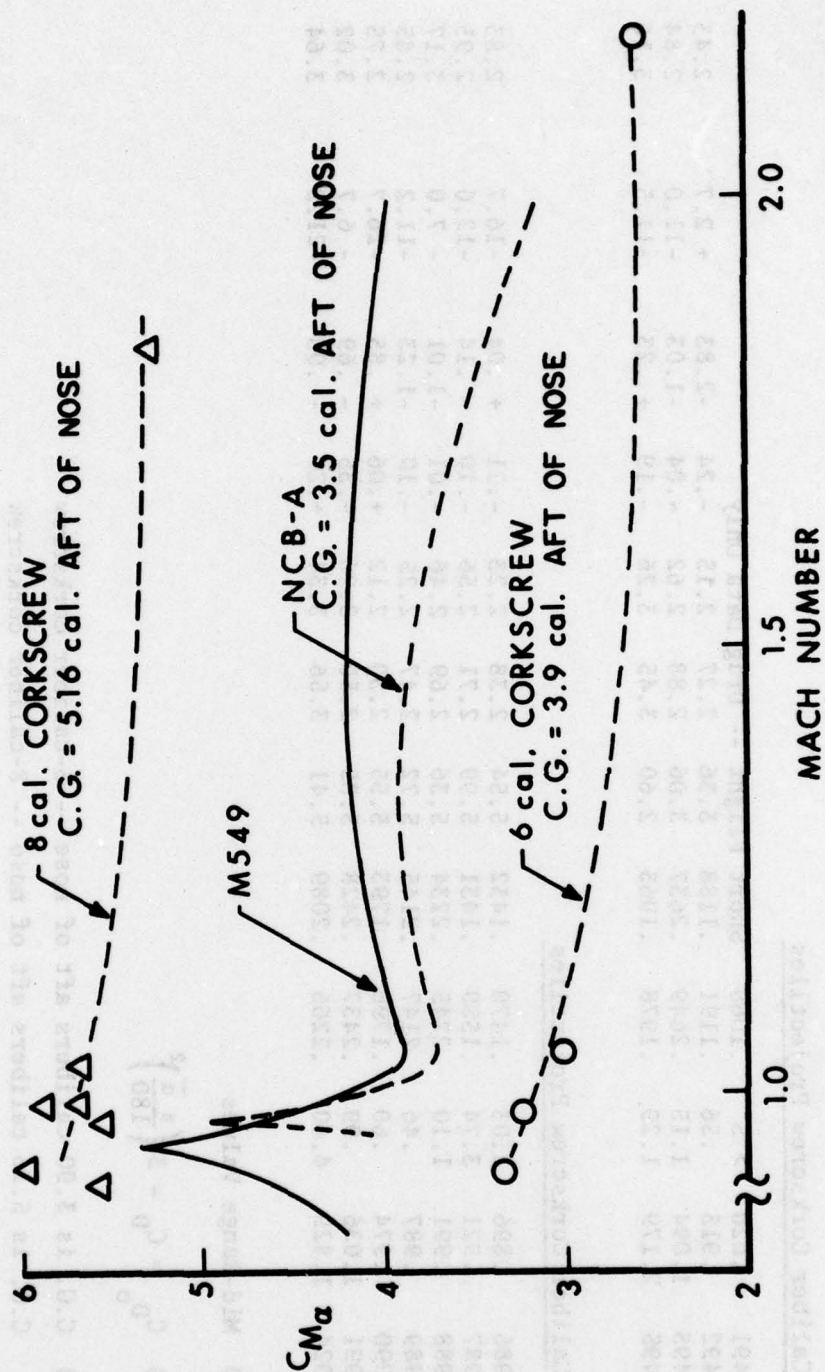


Figure 13. The Pitching Moment Coefficient of the Corkscrew Projectile Compared to Other Projectiles

Table I. Aerodynamic Characteristics of the 6-Caliber and 8-Caliber Corkscrews

(1) Round	Mach	$\bar{\alpha}$ Deg.	(2)		(3)		(3)		$C_{M_q} + C_{M_{\dot{\alpha}}}$	C.P.N Cal. Aft of Nose
			C_D	C_{D_o}	$C_{M_{\alpha}}$	$C_{N_{\alpha}}$	$C_{L_{\alpha}}$	$C_{M_{pa}}$		
6-Caliber Corkscrew Projectiles										
12491	.620	> 5°	.1068	Short Flight	-- Drag Data Only					
12492	.913	.56	.1191	.1188	3.36	2.27	2.15	-.24	-2.83	+ 2.7
12493	1.094	1.15	.2649	.2637	3.06	2.88	2.62	-.04	-1.03	-11.0
12495	2.179	1.29	.1978	.1963	2.60	3.45	3.26	-.19	+ .23	-11.5
										2.43
										2.84
										3.16
8-Caliber Corkscrew Projectiles										
12986	.896	2.03	.1470	.1432	5.54	2.38	2.23	-.21	+ .04	-16.7
12987	.921	3.74	.1559	.1431	5.99	2.71	2.56	-.10	-.14	-12.6
12988	.991	1.10	.2245	.2234	5.36	2.69	2.46	-.01	-1.01	-7.0
12989	.987	.46	.2147	.2145	5.72	2.47	2.25	-.19	-1.23	-11.2
12990	.974	.60	.1796	.1793	5.55	2.30	2.12	+.06	+.85	-26.7
12991	1.036	.99	.2437	.2428	5.35	2.50	2.26	-.35	-.69	-6.7
13024	1.829	4.40	.2266	.2089	5.41	3.56	3.34	+.20	-.08	-21.2
										2.83
										2.95
										3.17
										2.85
										2.75
										3.02
										3.64

(1) Mid-Range Values

$$(2) C_{D_o} = C_D - 3 \left(\frac{\pi \alpha^2}{180} \right)$$

(3) C.G. is 3.90 calibers aft of nose -- 6-caliber corkscrew
C.G. is 5.16 calibers aft of nose -- 8-caliber corkscrew

Table II. Aeroballistic Characteristics of the 6-Caliber and 8-Caliber Corkscrews

Round	S_g	S_d	$\lambda_F \times 10^3$ 1/Cal	$\lambda_S \times 10^3$ 1/Cal	K_F Rad	K_S Rad	ϕ'_F Rad/ Cal	ϕ'_S Rad/ Cal	Yaw Radius RMS Yaw Fit	Swerve Radius RMS Swerve Fit
6-Caliber Corkscrew										
12491	Short Flight	--	Drag Data Only							
12492	3.04	6.84	-.0176	+.0272	.0073	.0064	.0251	.00253	6.1	5.3 5.6 3.0
12493	3.45	.44	-.2450	-.0554	.0104	.0156	.0255	.00218	6.1	9.2 15.5 2.5
12495	4.31	.23	-.2839	-.1630	.0109	.0194	.0255	.00175	9.9	17.6 18.5 .5
8-Caliber Corkscrew										
12986	2.03	.06	-.2104	+.0369	.0182	.0301	.0137	.00285	4.8	7.9 5.7 .03
12987	1.64	.43	-.1393	.0077	.0399	.0511	.0135	.00309	17.3	22.2 10.5 .25
12988	2.02	.89	-.0521	-.0645	.0136	.0135	.0137	.00280	5.7	5.6 2.6 .5
12989	1.66	.10	-.1772	+.0196	.0037	.0070	.0142	.00289	1.3	2.5 1.6 .4
12990	1.71	.44	-.2338	-.0277	.0066	.0079	.0136	.00295	3.0	3.6 1.4 .25
12991	1.78	.53	-.1658	+.0542	.0093	.0145	.0139	.00276	3.9	6.0 3.3 .4
13024	1.93	.92	-.1299	-.1029	.0548	.0533	.0145	.00265	20.3	19.7 42.1 .5

Table III. Physical and Aerodynamic Characteristics

z/d	6	7	8	9	10	11
Vol/r^3	18.0	21.5	24.9	28.4	31.9	35.4
C.G.	3.90	4.53	5.16	5.79	6.43	7.06
$I_y/\rho_m r^5$	91.2	151.2	233.0	339.9	458.9	624.5
k_y	1.13	1.33	1.53	1.73	1.90	2.10
$I_x/\rho_m r^5$	6.48	7.85	9.23	10.60	11.97	13.35
k_x	.300	.302	.304	.305	.306	.307
For Mach Number = 2.1 and Spin = 1/15 cal.						
C_{N_α} (estimated)	3.4		3.4		3.2	3.2
C_{M_α} (estimated)	2.58		4.08		5.69	6.28
s_g	3.73		2.27		1.39	1.15

REFERENCES

1. Anders S. Platou, "An Improved Projectile Boattail," Ballistic Research Laboratory Memorandum Report No. 2395, July 1974. AD 785520.
2. Anders S. Platou and George I. T. Nielsen, "An Improved Projectile Boattail. Part II," Ballistic Research Laboratory Report No. 1866, March 1976. AD A024073.
3. Anders S. Platou, "An Improved Projectile Boattail. Part III," Ballistic Research Laboratory Memorandum Report No. 2644, July 1976. AD B012781L.
4. John H. Whiteside, "Transonic Tests of the 155mm Non-Conical Boat-tail Projectile A and 8-Inch XM650E4 and EBVP Projectiles at Nicolet, Canada, During January-February 1977," Ballistic Research Laboratory Memorandum Report No. ARBRL-MR-02809, January 1978.
5. Vural Oskay and Anders S. Platou, "Yawsonde Tests of 155mm M549 Non-Conical Boattail Projectile at Tonopah Test Range," Ballistic Research Laboratory Memorandum Report in preparation.
6. Anders S. Platou, "Wind Tunnel, Aeroballistic Range, and Full Range Flight Tests of the Non-Conical Boattail Projectile A," Ballistic Research Laboratory Memorandum Report in preparation.

LIST OF SYMBOLS

C_D	$\frac{\text{Drag}}{\frac{1}{2} \rho V^2 S}$;	positive direction is aft
C_{D_0}		zero angle-of-attack drag coefficient
C.G.		center of gravity, calibers aft of nose
C_{L_α}	$\frac{\text{Lift Force}}{\frac{1}{2} \rho V^2 S}$;	positive direction is up
C_M	$\frac{\text{Pitching Moment}}{\frac{1}{2} \rho V^2 S d}$;	positive moment is due to positive normal force ahead of the moment center
C_{M_α}	$\frac{d C_M}{d \alpha}$	at $\alpha = 0$ per radian
C_{M_p}	$\frac{\text{Magnus Moment}}{\frac{1}{2} \rho V^2 S d \frac{pd}{V}}$;	positive moment is due to positive Magnus force ahead of moment center
$C_{M_{p\alpha}}$	$\frac{d C_{M_p}}{d \alpha}$	at $\alpha = 0$ per radian
$C_{M_q} + C_{M_{\dot{\alpha}}}$	$\frac{\text{Damping Moment}}{\frac{1}{2} \rho V^2 S d \frac{ q_{\dot{\alpha}} d}{V}}$	
C_N	$\frac{\text{Normal Force}}{\frac{1}{2} \rho V^2 S}$;	positive direction is up
C_{N_α}	$\frac{d C_N}{d \alpha}$	at $\alpha = 0$ per radian
C_{N_p}	$\frac{\text{Magnus Force}}{\frac{1}{2} \rho V^2 S \frac{pd}{V}}$;	positive direction is to right looking upstream

LIST OF SYMBOLS (Continued)

$C_{N_{pa}}$	$\frac{d C_N}{d \alpha} p$ at $\alpha = 0$ per radian
C.P. _N	normal force center of pressure
d	projectile diameter
I_x	axial moment of inertia
I_y	transverse moment of inertia
k_x	axial radius of gyration
k_y	transverse radius of gyration
K_F	length of fast arm in epicyclic motion
K_S	length of slow arm in epicyclic motion
m	projectile mass
M	Mach number
p	projectile spin, rad/sec (positive is clockwise looking upstream)
q_t	complex transverse angular velocity
r	projectile radius = $\frac{d}{2}$
S	body area = $\frac{\pi d^2}{4}$
s_d	dynamic stability = $\frac{2 (C_{L_\alpha} + k_x^{-2} C_{m_{pa}})}{C_{L_\alpha} - C_D - k_y^{-2} (C_{M_q} + C_{M_{\dot{\alpha}}})}$

LIST OF SYMBOLS (Continued)

s_g	gyroscopic stability = $\frac{\left(\frac{I_x}{I_y}\right)^2 \left(\frac{pd}{V}\right)^2}{4 \frac{\rho S d^3}{2 I_y} C_{M_\alpha}}$
V	magnitude of the free stream velocity
α	angle of attack
$\bar{\alpha}_t$	mean angle of attack during each flight
δ	cant angle of fin or twisted surface
ρ	free stream air density
ρ_m	projectile mass
λ_F	damping rate of fast arm in epicyclic motion
λ_S	damping rate of slow arm in epicyclic motion
ϕ'_F	rotational rate of fast arm in epicyclic motion
ϕ'_S	rotational rate of slow arm in epicyclic motion

DISTRIBUTION LIST

<u>No. of</u> <u>Copies</u>	<u>Organization</u>	<u>No. of</u> <u>Copies</u>	<u>Organization</u>
12	Commander Defense Documentation Center ATTN: DDC-TCA Cameron Station Alexandria, Virginia 22314	1	Commander US Army Tank Automotive Research and Development Command ATTN: DRDTA-RWL Warren, Michigan 48090
1	Commander US Army Materiel Development and Readiness Command ATTN: DRCDMA-ST 5001 Eisenhower Avenue Alexandria, Virginia 22333	2	Commander US Army Mobility Equipment Research and Development Command ATTN: Tech Docu Cen, Bldg. 315 DRSME-RZT Fort Belvoir, Virginia 22060
1	Commander US Army Aviation Research and Development Command ATTN: DRSAR-E 12th and Spruce Streets St. Louis, Missouri 63166	1	Commander US Army Armament Materiel Readiness Command ATTN: DRSAR-LEP-L, Tech Lib Rock Island, Illinois 61202
1	Director US Army Air Mobility Research and Development Laboratory Ames Research Center Moffett Field, CA 94035	5	Commander US Army Armament Research and Development Command ATTN: DRDAR-TSS DRDAR-LCA-F Mr. S. Wasserman Mr. D. Mertz Mr. E. Falkowski Mr. A. Loeb Dover, NJ 07801
1	Commander US Army Electronics Command ATTN: DRSEL-RD Fort Monmouth, NJ 07703	1	Commander US Army Harry Diamond Laboratories ATTN: DRXDO-TI 2800 Powder Mill Road Adelphi, Maryland 20783
1	Commander US Army Jefferson Proving Ground ATTN: STEJP-TD-D Madison, Indiana 47250	1	Commander US Army Natick Research and Development Command ATTN: DRXRE, Dr. D. Sieling Natick, Massachusetts 01762
4	Commander US Army Missile Research and Development Command ATTN: DRDMI-R DRDMI-T DRDMI-TD, Mr. R. Becht Mr. R. Deep Redstone Arsenal, AL 35809		

DISTRIBUTION LIST

<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>
1	Director US Army TRADOC Systems Analysis Activity ATTN: ATAA-SL, Tech Lib White Sands Missile Range New Mexico 88002	1	Arnold Research Organization, Inc. von Karman Gas Dynamics Facility ATTN: Dr. John C. Adams, Jr. Aerodynamics Division Projects Branch Arnold AFS, Tennessee 37389
1	Commander US Army Research Office P.O. Box 12211 Research Triangle Park North Carolina 27709	1	Calspan Corporation ATTN: Mr. J. Andes, Head Transonic Tunnel Dept. P.O. Box 235 Buffalo, New York 14221
3	Commander US Naval Air Systems Command ATTN: AIR-604 Washington, D. C. 20360	1	Honeywell, Inc. ATTN: Mr. George Stilley 600 Second Street, N. Hopkins, Minnesota 55343
2	Commander David W. Taylor US Naval Ship Research and Development Center ATTN: Dr. S. de los Santos Mr. Stanley Gottlieb Bethesda, Maryland 20084	1	Sandia Laboratories ATTN: Division No. 1331 Mr. H. R. Vaughn P.O. Box 5800 Albuquerque, New Mexico 87115
1	Commander US Naval Surface Weapons Center ATTN: Dr. T. Clare, Code DK20 Dahlgren, Virginia 22448	2	Massachusetts Institute of Technology ATTN: Prof. E. Covert Prof. C. Haldeman 77 Massachusetts Avenue Cambridge, Massachusetts 02139
2	Commander US Naval Surface Weapons Center ATTN: Code 312, Mr. S. Hastings Code 312, Mr. F. Regan Silver Spring, Maryland 20910	1	MIT/Lincoln Laboratories ATTN: Dr. Milan Vlainiac Mail Stop D-382 P.O. Box 73 Lexington, MA 02173
1	Commander US Naval Weapons Center ATTN: Code 5115 Dr. A. Charters China Lake, California 93555	1	Rutgers University Mechanical, Industrial, and Aerospace Engineering Department ATTN: Dr. Robert H. Page New Brunswick, NJ 08903
1	AFATL (DLDL) Eglin AFB, Florida 32542		

DISTRIBUTION LIST

No. of
Copies

Organization

1 University of Virginia
Department of Aerospace
Engineering and Engineering
Physics
ATTN: Prof. I. Jacobson
Charlottesville, Virginia 22904

Aberdeen Proving Ground

Marine Corps Ln Ofc
Director, USAMSAA

ED
78